

# Webinar Series in Applied Quantitative Analysis

| Date               | Topic                                                                       |
|--------------------|-----------------------------------------------------------------------------|
|                    | <u>Session One</u>                                                          |
| <b>February 29</b> | Potential Outcomes and Omitted Variable Bias I (Theory)                     |
| <b>March 7</b>     | Potential Outcomes and Omitted Variable Bias II (Application)               |
|                    | <u>Session Two</u>                                                          |
| <b>March 21</b>    | Difference-in-differences I (Theory)                                        |
| <b>March 28</b>    | Difference-in-differences II (Application)                                  |
|                    | <u>Session Three</u>                                                        |
| <b>April 25</b>    | Power analysis, clustering and sample size calculations I (Theory)          |
| <b>May 2</b>       | Power analysis, clustering and sample size calculations II (Application)    |
|                    | <u>Session Four</u>                                                         |
| <b>May 23</b>      | Fixed-effects I (Theory)                                                    |
| <b>May 30</b>      | Fixed-effects II (Application)                                              |
|                    | <u>Session Five</u>                                                         |
| <b>June 20</b>     | Instrumental variables I (Theory)                                           |
| <b>June 27</b>     | Instrumental Variables II (Application)                                     |
|                    | <u>Session Six</u>                                                          |
| <b>July 25</b>     | Lagged dependent variables and the Arellano-Bond Estimator I (Theory)       |
| <b>August 1</b>    | Lagged dependent variables and the Arellano-Bond Estimator II (Application) |

# Series Objectives and Target Audience

- Cover methods and issues commonly faced by social scientists when doing empirical work
  - We are open to suggestions for topics, if there is demand, we can continue the series next year
- Target audience is post-graduate students in African universities
  - Economics, Sociology, Agriculture, Population Studies and related fields
  - Anyone with an interest in empirical work and causal inference
  - Must have taken regression and statistics for this to be beneficial to you
- The structure is like a classroom, we will teach theory and then provide examples and demonstrations
  - The first session today, and some of the others, will likely be refreshers

# Logistics and other topics

- Participants are muted, chat is disabled, write questions in the Q&A box
  - Selected questions will be answered and posted publicly during the webinar, all Q&A will be posted on the webinar website after the session + video of the session
  - Occasionally we will open the chat to receive responses to questions posed
- You can attend any webinar you want, topics are independent and do not build on each other like a structured course
  - But the first week's topic is an important base to better understand subsequent topics
  - Registration link again: [https://air-org.zoom.us/webinar/register/WN\\_MJ5UevG-RESBb-iWtEOdmQ](https://air-org.zoom.us/webinar/register/WN_MJ5UevG-RESBb-iWtEOdmQ)
- We will have a guest speaker for topics 4 and 5 (FE and IV) and maybe others
  - Paul Sirma is handling the Q&A; Jacque Ngao the logistics, Isaac Kiplagat the IT stuff

# Selection bias in regression: Linking omitted variable bias with the potential outcomes framework

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Institute Fellow – AIR

Kenan Eminent Professor of Public Policy, UNC-CH

# Modern econometrics is about counterfactual thinking

- Move away from ‘goodness of fit’ and model fitting towards a focus on point estimates and unbiasedness
  - Focus on causal inference
- In this framework the variable of interest can be viewed as a ‘treatment’ which then helps us identify the counterfactual
- Then we ask—is there selection bias? Why or how?
- Use toolkit to resolve the selection bias (experimental designs, fixed-effects, difference-in-differences, etc)

We will link the ‘potential outcomes framework’ (next week) to what we learned in econometrics class—bias in the OLS regression model

Selection can be viewed as an omitted variable which leads to bias

- frailty or the health endowment
- innate ability or special knowledge (master farmers)
- motivation, industriousness

In impact evaluation, selection into program participation is the concern

In general applications, we want to understand whether we have a good counterfactual and if not, find ways to improve it

Housing spending in the U.S. – do renters pay more than non-renters?

Renters pay 8.1% less than non-renters controlling for family size and race

```
. reg log_h renter fam_size white black
```

| Source   | SS         | df     | MS         | Number of obs | = | 16,219 |
|----------|------------|--------|------------|---------------|---|--------|
| Model    | 979.660909 | 4      | 244.915227 | F(4, 16214)   | = | 341.13 |
| Residual | 11640.8373 | 16,214 | .717949754 | Prob > F      | = | 0.0000 |
|          |            |        |            | R-squared     | = | 0.0776 |
|          |            |        |            | Adj R-squared | = | 0.0774 |
| Total    | 12620.4982 | 16,218 | .778178458 | Root MSE      | = | .84732 |

| log_housing | Coefficient | Std. err. | t      | P> t  | [95% conf. interval] |           |
|-------------|-------------|-----------|--------|-------|----------------------|-----------|
| renter      | -.0812318   | .0141718  | -5.73  | 0.000 | -.1090101            | -.0534535 |
| fam_size    | .1537796    | .0045256  | 33.98  | 0.000 | .144909              | .1626502  |
| white       | -.1304967   | .0260013  | -5.02  | 0.000 | -.1814622            | -.0795312 |
| black       | -.2704562   | .0316689  | -8.54  | 0.000 | -.3325307            | -.2083818 |
| _cons       | 7.222598    | .0288747  | 250.14 | 0.000 | 7.166001             | 7.279196  |

Renters pay 9.3% less than non-renters controlling for family size and race and region of residence

Is there selection bias? (Not really—the coefficient of ‘renter’ hardly changed)

Renters are equally as likely to live in urban and rural areas: No selection into urban/rural

```
. reg log_h renter fam_size white black urban
```

| Source   | SS         | df     | MS         | Number of obs | = | 16,219 |
|----------|------------|--------|------------|---------------|---|--------|
| Model    | 1246.70862 | 5      | 249.341723 | F(5, 16213)   | = | 355.43 |
| Residual | 11373.7896 | 16,213 | .701522828 | Prob > F      | = | 0.0000 |
|          |            |        |            | R-squared     | = | 0.0988 |
|          |            |        |            | Adj R-squared | = | 0.0985 |
| Total    | 12620.4982 | 16,218 | .778178458 | Root MSE      | = | .83757 |

| log_housing | Coefficient | Std. err. | t      | P> t  | [95% conf. interval] |           |
|-------------|-------------|-----------|--------|-------|----------------------|-----------|
| renter      | -.0934233   | .0140227  | -6.66  | 0.000 | -.1209092            | -.0659373 |
| fam_size    | .1527183    | .0044738  | 34.14  | 0.000 | .1439491             | .1614875  |
| white       | -.097098    | .0257591  | -3.77  | 0.000 | -.1475886            | -.0466073 |
| black       | -.266627    | .0313051  | -8.52  | 0.000 | -.3279884            | -.2052655 |
| urban       | .4901121    | .0251201  | 19.51  | 0.000 | .4408739             | .5393503  |
| _cons       | 6.748645    | .0374803  | 180.06 | 0.000 | 6.675179             | 6.82211   |

Renters pay 11.9% MORE than non-renters controlling for family size and race and region of residence and income

Is there selection bias? Yes—the coefficient of ‘renter’ completely flipped signs  
There is differential selection into income for renters and non-renters. Do renters select into ‘low’ or ‘high’ income?

```
. reg log_h renter fam_size white black urban log_pc
```

| Source   | SS         | df     | MS         | Number of obs | = | 16,219 |
|----------|------------|--------|------------|---------------|---|--------|
|          |            |        |            | F(6, 16212)   | = | 898.23 |
| Model    | 3148.72697 | 6      | 524.787828 | Prob > F      | = | 0.0000 |
| Residual | 9471.77126 | 16,212 | .584244464 | R-squared     | = | 0.2495 |
|          |            |        |            | Adj R-squared | = | 0.2492 |
| Total    | 12620.4982 | 16,218 | .778178458 | Root MSE      | = | .76436 |

| log_housing | Coefficient | Std. err. | t     | P> t  | [95% conf. interval] |           |
|-------------|-------------|-----------|-------|-------|----------------------|-----------|
| renter      | .1187369    | .0133262  | 8.91  | 0.000 | .092616              | .1448578  |
| fam_size    | .2094188    | .004202   | 49.84 | 0.000 | .2011824             | .2176551  |
| white       | -.0578265   | .0235176  | -2.46 | 0.014 | -.1039236            | -.0117294 |
| black       | -.1350735   | .0286616  | -4.71 | 0.000 | -.1912535            | -.0788935 |
| urban       | .3203993    | .0231166  | 13.86 | 0.000 | .2750882             | .3657103  |
| log_pcinc   | .3999453    | .0070096  | 57.06 | 0.000 | .3862058             | .4136848  |
| _cons       | 2.658703    | .079424   | 33.47 | 0.000 | 2.503023             | 2.814383  |

# Omitted variable bias formula from our OLS regression class helps us understand selection

- We will show some math for the sake of transparency and completeness, and so you have notes but this is not a math class
- Focus on the intuition, and how to use the bias formula in practice (we will do some examples)

# OLS regression refresher (before entering into omitted variable bias)

*For  $Z_i = \gamma_0 + \gamma_1 P + \sigma_i$  the OLS estimator of  $\gamma_1$  is given by*

$$\hat{\gamma}_1 = \frac{\sum (P_i - \bar{P}) Z_i}{\sum (P_i - \bar{P})^2} = \frac{COV(P, Z)}{VAR(P)} \quad (\text{check notes from econometrics class})$$

- *“Covariance between the outcome and the predictor divided by the variance of the predictor”*
- Remember this formula, will be used later

# Omitted variable bias in classical regression

$$Y_i = \beta_0 + \beta_1 P + \beta_2 Z + \mu_i \quad \text{True relationship}$$

$$Y_i = \alpha_0 + \alpha_1 P + \varepsilon_i \quad \text{Estimated relationship (Z omitted)}$$

From previous slide, recall that OLS estimate of  $\alpha_1$  is given by “*covariance between outcome and predictor divided by variance of the predictor*”

$$\widehat{\alpha_1} = \frac{\sum (P_i - \bar{P}) Y_i}{\sum (P_i - \bar{P})^2} = \frac{COV(P, Y)}{VAR(P)}$$

Substitute for  $Y_i$  using true equation

$$\widehat{\alpha}_1 = \frac{\sum(P_i - \bar{P})Y_i}{\sum(P_i - \bar{P})^2} = \frac{\sum(P_i - \bar{P})(\beta_0 + \beta_1 P_i + \beta_2 Z_i + \mu_i)}{\sum(P_i - \bar{P})^2}$$

$$\widehat{\alpha}_1 = \frac{\beta_0 \sum(P_i - \bar{P})}{\sum(P_i - \bar{P})^2} + \frac{\beta_1 \sum(P_i - \bar{P})P_i}{\sum(P_i - \bar{P})^2} + \frac{\beta_2 \sum(P_i - \bar{P})Z_i}{\sum(P_i - \bar{P})^2} + \frac{\sum(P_i - \bar{P})\mu_i}{\sum(P_i - \bar{P})^2}$$

Expand the numerator

Substitute for  $Y_i$  using true equation

$$\bullet \hat{\alpha}_1 = \frac{\sum(P_i - \bar{P})Y_i}{\sum(P_i - \bar{P})^2} = \frac{\sum(P_i - \bar{P})(\beta_0 + \beta_1 P_i + \beta_2 Z_i + \mu_i)}{\sum(P_i - \bar{P})^2}$$

Expand the numerator

$$\bullet \hat{\alpha}_1 = \frac{\beta_0 \sum(P_i - \bar{P})}{\sum(P_i - \bar{P})^2} + \frac{\beta_1 \sum(P_i - \bar{P})P_i}{\sum(P_i - \bar{P})^2} + \frac{\beta_2 \sum(P_i - \bar{P})Z_i}{\sum(P_i - \bar{P})^2} + \frac{\sum(P_i - \bar{P})\mu_i}{\sum(P_i - \bar{P})^2}$$

Substitute for  $Y_i$  using true equation

$$\bullet \hat{\alpha}_1 = \frac{\sum(P_i - \bar{P})Y_i}{\sum(P_i - \bar{P})^2} = \frac{\sum(P_i - \bar{P})(\beta_0 + \beta_1 P_i + \beta_2 Z_i + \mu_i)}{\sum(P_i - \bar{P})^2}$$

Expand the numerator

$$\bullet \hat{\alpha}_1 = \frac{\beta_0 \sum(P_i - \bar{P})}{\sum(P_i - \bar{P})^2} + \frac{\beta_1 \sum(P_i - \bar{P})P_i}{\sum(P_i - \bar{P})^2} + \frac{\beta_2 \sum(P_i - \bar{P})Z_i}{\sum(P_i - \bar{P})^2} + \frac{\sum(P_i - \bar{P})\mu_i}{\sum(P_i - \bar{P})^2}$$

Substitute for  $Y_i$  using true equation

$$\bullet \hat{\alpha}_1 = \frac{\sum(P_i - \bar{P})Y_i}{\sum(P_i - \bar{P})^2} = \frac{\sum(P_i - \bar{P})(\beta_0 + \beta_1 P_i + \beta_2 Z_i + \mu_i)}{\sum(P_i - \bar{P})^2}$$

Expand the numerator

$$\bullet \hat{\alpha}_1 = \frac{\beta_0 \sum(P_i - \bar{P})}{\sum(P_i - \bar{P})^2} + \frac{\beta_1 \sum(P_i - \bar{P})P_i}{\sum(P_i - \bar{P})^2} + \frac{\beta_2 \sum(P_i - \bar{P})Z_i}{\sum(P_i - \bar{P})^2} + \frac{\sum(P_i - \bar{P})\mu_i}{\sum(P_i - \bar{P})^2}$$

Substitute for  $Y_i$  using true equation

$$\bullet \hat{\alpha}_1 = \frac{\sum(P_i - \bar{P})Y_i}{\sum(P_i - \bar{P})^2} = \frac{\sum(P_i - \bar{P})(\beta_0 + \beta_1 P_i + \beta_2 Z_i + \mu_i)}{\sum(P_i - \bar{P})^2}$$

Expand the numerator

$$\bullet \hat{\alpha}_1 = \frac{\beta_0 \sum(P_i - \bar{P})}{\sum(P_i - \bar{P})^2} + \frac{\beta_1 \sum(P_i - \bar{P})P_i}{\sum(P_i - \bar{P})^2} + \frac{\beta_2 \sum(P_i - \bar{P})Z_i}{\sum(P_i - \bar{P})^2} + \frac{\sum(P_i - \bar{P})\mu_i}{\sum(P_i - \bar{P})^2}$$

$$\hat{\alpha}_1 = \frac{\beta_0 \sum(P_i - \bar{P})}{\sum(P_i - \bar{P})^2} + \frac{\beta_1 \sum(P_i - \bar{P})P_i}{\sum(P_i - \bar{P})^2} + \frac{\beta_2 \sum(P_i - \bar{P})Z_i}{\sum(P_i - \bar{P})^2} + \frac{\sum(P_i - \bar{P})\mu_i}{\sum(P_i - \bar{P})^2}$$

Sum of deviations from  
mean is simply = 0

$$\hat{\alpha}_1 = \frac{\beta_0 \sum (P_i - \bar{P})}{\sum (P_i - \bar{P})^2} + \frac{\beta_1 \sum (P_i - \bar{P}) P_i}{\sum (P_i - \bar{P})^2} + \frac{\beta_2 \sum (P_i - \bar{P}) Z_i}{\sum (P_i - \bar{P})^2} + \frac{\sum (P_i - \bar{P}) \mu_i}{\sum (P_i - \bar{P})^2}$$

Sum of deviations from  
mean is simply = 0

Can be shown that this is =  
 $\sum (P_i - \bar{P})^2$ , same as denominator

$$\hat{\alpha}_1 = \frac{\beta_0 \sum (P_i - \bar{P})}{\sum (P_i - \bar{P})^2} + \frac{\beta_1 \sum (P_i - \bar{P}) P_i}{\sum (P_i - \bar{P})^2} + \frac{\beta_2 \sum (P_i - \bar{P}) Z_i}{\sum (P_i - \bar{P})^2} + \frac{\sum (P_i - \bar{P}) \mu_i}{\sum (P_i - \bar{P})^2}$$

Sum of deviations from mean is simply = 0

Can be shown that this is =  $\sum (P_i - \bar{P})^2$ , same as denominator

$\text{COV}(P_i, \mu_i) = 0$  by OLS assumption

$$\hat{\alpha}_1 = \frac{\beta_0 \sum (P_i - \bar{P})}{\sum (P_i - \bar{P})^2} + \frac{\beta_1 \sum (P_i - \bar{P}) P_i}{\sum (P_i - \bar{P})^2} + \frac{\beta_2 \sum (P_i - \bar{P}) Z_i}{\sum (P_i - \bar{P})^2} + \frac{\sum (P_i - \bar{P}) \mu_i}{\sum (P_i - \bar{P})^2}$$

Sum of deviations from mean is simply = 0

Can be shown that this is =  $\sum (P_i - \bar{P})^2$ , same as denominator

$\text{COV}(P_i, \mu_i) = 0$  by OLS assumption

$$\hat{\alpha}_1 = \beta_1 + \frac{\beta_2 \sum (P_i - \bar{P}) Z_i}{\sum (P_i - \bar{P})^2}$$

When we estimate (2) and the true relationship is (1)

$$(1) \quad Y_i = \beta_0 + \beta_1 P + \beta_2 Z + \mu_i \quad \text{True relationship}$$

$$(2) \quad Y_i = \alpha_0 + \alpha_1 P + \varepsilon_i \quad \text{Estimated relationship (Z omitted)}$$

We discover that the OLS estimate of  $\alpha_1$  is given by

$$\widehat{\alpha}_1 = \beta_1 + \frac{\beta_2 \sum (P_i - \bar{P}) Z_i}{\sum (P_i - \bar{P})^2}$$

When we estimate (2) and the true relationship is (1)

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We discover that the OLS estimate of  $\alpha_1$  is given by

$$\widehat{\alpha}_1 = \beta_1 + \beta_2 \frac{\sum (P_i - \bar{P}) Z_i}{\sum (P_i - \bar{P})^2} = \beta_1 + \beta_2 \frac{COV(P, Z)}{VAR(P)}$$

Do you recognize this?

# Refresher of 'OLS regression refresher'

*For  $Z_i = \gamma_0 + \gamma_1 P + \sigma_i$  the OLS estimator of  $\gamma_1$  is given by*

$$\hat{\gamma}_1 = \frac{\sum (P_i - \bar{P}) Z_i}{\sum (P_i - \bar{P})^2} = \frac{COV(P, Z)}{VAR(P)} \quad (\text{see slide 3})$$

# Refresher of 'OLS regression refresher'

For  $Z_i = \gamma_0 + \gamma_1 P + \sigma_i$  the OLS estimator of  $\gamma_1$  is given by

$$\hat{\gamma}_1 = \frac{\sum (P_i - \bar{P}) Z_i}{\sum (P_i - \bar{P})^2} = \frac{COV(P, Z)}{VAR(P)} \quad (\text{see slide 3})$$


$$\hat{\alpha}_1 = \beta_1 + \beta_2 \frac{COV(P, Z)}{VAR(P)} = \beta_1 + \beta_2 * \boxed{\hat{\gamma}_1}$$

When we estimate (2) and the true relationship is (1)

$$(1) \quad Y_i = \beta_0 + \beta_1 P + \beta_2 Z + \mu_i \quad \text{True relationship}$$

$$(2) \quad Y_i = \alpha_0 + \alpha_1 P + \varepsilon_i \quad \text{Estimated relationship (Z omitted)}$$

Then the estimate of  $\alpha_1$  is given by

$$\hat{\alpha}_1 = \beta_1 + \beta_2 * \hat{\gamma}_1$$

“The omitted variable bias formula” or “the bias formula”

“The most important formula of your PhD career”

When we estimate (2) and the true relationship is (1)

$$(1) \quad Y_i = \beta_0 + \beta_1 P + \beta_2 Z + \mu_i \quad \text{True relationship}$$

$$(2) \quad Y_i = \alpha_0 + \alpha_1 P + \varepsilon_i \quad \text{Estimated relationship (Z omitted)}$$

Then the estimate of  $\alpha_1$  is given by

$$\widehat{\alpha}_1 = \beta_1 + \beta_2 * \widehat{\gamma}_1$$

The diagram illustrates the decomposition of the estimated coefficient  $\widehat{\alpha}_1$  into two components. The first component,  $\beta_1$ , is labeled as the 'True 'impact' of P on Y'. The second component,  $\beta_2 * \widehat{\gamma}_1$ , is labeled as 'Selection bias'. The term  $\beta_2 * \widehat{\gamma}_1$  is highlighted with a red box in the original image.

When we estimate (2) and the true relationship is (1)

$$(1) \quad Y_i = \beta_0 + \beta_1 P + \beta_2 Z + \mu_i \quad \text{True relationship}$$

$$(2) \quad Y_i = \alpha_0 + \alpha_1 P + \varepsilon_i \quad \text{Estimated relationship (Z omitted)}$$

The sources of bias:

$$\widehat{\alpha}_1 = \beta_1 + \beta_2 * \widehat{\gamma}_1$$

Selection bias has two elements

$\beta_2$  = the relationship between the excluded variable (Z) and the outcome (Y)

$\gamma_1$  = the relationship between the excluded variable (Z) and included variable (P)

Back to our example of the determinants of house spending in the U.S.

Renters pay 9.3% less than non-renters controlling for family size and race and region of residence

```
. reg log_h renter fam_size white black urban
```

| Source   | SS         | df     | MS         | Number of obs | = | 16,219 |
|----------|------------|--------|------------|---------------|---|--------|
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|          |            |        |            | Adj R-squared | = | 0.0985 |
| Total    | 12620.4982 | 16,218 | .778178458 | Root MSE      | = | .83757 |

| log_housing | Coefficient | Std. err. | t      | P> t  | [95% conf. interval] |           |
|-------------|-------------|-----------|--------|-------|----------------------|-----------|
| renter      | -.0934233   | .0140227  | -6.66  | 0.000 | -.1209092            | -.0659373 |
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| white       | -.097098    | .0257591  | -3.77  | 0.000 | -.1475886            | -.0466073 |
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| _cons       | 6.748645    | .0374803  | 180.06 | 0.000 | 6.675179             | 6.82211   |

-After controlling income, coefficient goes from -.093 to +.119 (an increase of 0.212)

-Use the bias formula to understand selection bias in this case

```
. reg log_h renter fam_size white black urban log_pc
```

| Source   | SS         | df     | MS         | Number of obs | = | 16,219 |
|----------|------------|--------|------------|---------------|---|--------|
| Model    | 3148.72697 | 6      | 524.787828 | F(6, 16212)   | = | 898.23 |
| Residual | 9471.77126 | 16,212 | .584244464 | Prob > F      | = | 0.0000 |
|          |            |        |            | R-squared     | = | 0.2495 |
|          |            |        |            | Adj R-squared | = | 0.2492 |
| Total    | 12620.4982 | 16,218 | .778178458 | Root MSE      | = | .76436 |

| log_housing | Coefficient | Std. err. | t     | P> t  | [95% conf. interval] |           |
|-------------|-------------|-----------|-------|-------|----------------------|-----------|
| renter      | .1187369    | .0133262  | 8.91  | 0.000 | .092616              | .1448578  |
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| black       | -.1350735   | .0286616  | -4.71 | 0.000 | -.1912535            | -.0788935 |
| urban       | .3203993    | .0231166  | 13.86 | 0.000 | .2750882             | .3657103  |
| log_pcinc   | .3999453    | .0070096  | 57.06 | 0.000 | .3862058             | .4136848  |
| _cons       | 2.658703    | .079424   | 33.47 | 0.000 | 2.503023             | 2.814383  |

-Bias formula:  $\text{estimated coefficient} = \text{true coefficient} + \text{COV}(Y,Z) * \text{COV}(Z,P)$

-Bias formula:  $-0.093 = .119 + \{\text{COV}(\text{income, house spending}) * \text{COV}(\text{income, renter})\}$

$-0.093 = .119 + \{ \quad (+) \quad * \quad (-) \quad \}$

$-0.093 = .119 + \{-.212\}$

**-Large negative selection bias** (renters have significantly lower income than non-renters)

```
. reg log_h renter fam_size white black urban log_pc
```

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| Residual | 9471.77126 | 16,212 | .584244464 | Prob > F      | = | 0.0000 |
| Total    | 12620.4982 | 16,218 | .778178458 | R-squared     | = | 0.2495 |
|          |            |        |            | Adj R-squared | = | 0.2492 |
|          |            |        |            | Root MSE      | = | .76436 |

| log_housing | Coefficient | Std. err. | t     | P> t  | [95% conf. interval] |           |
|-------------|-------------|-----------|-------|-------|----------------------|-----------|
| renter      | .1187369    | .0133262  | 8.91  | 0.000 | .092616              | .1448578  |
| fam_size    | .2094188    | .004202   | 49.84 | 0.000 | .2011824             | .2176551  |
| white       | -.0578265   | .0235176  | -2.46 | 0.014 | -.1039236            | -.0117294 |
| black       | -.1350735   | .0286616  | -4.71 | 0.000 | -.1912535            | -.0788935 |
| urban       | .3203993    | .0231166  | 13.86 | 0.000 | .2750882             | .3657103  |
| log_pcinc   | .3999453    | .0070096  | 57.06 | 0.000 | .3862058             | .4136848  |
| _cons       | 2.658703    | .079424   | 33.47 | 0.000 | 2.503023             | 2.814383  |

```
. reg chldlabour attending_n male pcincome if ML_ZNZ==1
```

| Source   | SS         | df     | MS         | Number of obs | = | 11,617 |
|----------|------------|--------|------------|---------------|---|--------|
| Model    | 276.630299 | 3      | 92.2100997 | F(3, 11613)   | = | 549.12 |
| Residual | 1950.09278 | 11,613 | .167923257 | Prob > F      | = | 0.0000 |
|          |            |        |            | R-squared     | = | 0.1242 |
|          |            |        |            | Adj R-squared | = | 0.1240 |
| Total    | 2226.72308 | 11,616 | .19169448  | Root MSE      | = | .40978 |

| chldlabour    | Coefficient | Std. err. | t      | P> t  | [95% conf. interval] |           |
|---------------|-------------|-----------|--------|-------|----------------------|-----------|
| attending_now | -.4080822   | .0101163  | -40.34 | 0.000 | -.427912             | -.3882525 |
| male          | .0272711    | .007605   | 3.59   | 0.000 | .012364              | .0421783  |
| pcincome      | -7.73e-09   | 4.95e-09  | -1.56  | 0.118 | -1.74e-08            | 1.97e-09  |
| _cons         | .5843696    | .0099986  | 58.45  | 0.000 | .5647706             | .6039686  |

- TZ Labour Force Survey: Among children age 6-17, current enrollment is associated with 40.8 percentage point lower probability of child labour (linear probability model)
- We forgot to control for age—omitted variable bias
- What is the direction of bias? Is -40.8 too low or too high?

$$\widehat{\alpha}_1 = \beta_1 + \beta_2 * \widehat{\gamma}_1$$

$$-40.8 = \text{true} + \{\text{COV}(Z,Y)*\text{COV}(Z,P)\}$$

$$-40.8 = \text{true} + \{\text{COV}(\text{age, labor})*\text{COV}(\text{age, schooling})\}$$

- What is the correlation between age and child labor? negative or positive?
- What is the correlation between age and schooling? negative or positive?
- Is -40.80 too high or too low?

```
. reg chldlabour attending_n male age pcincome if ML_ZNZ==1
```

|          |            |        |            |               |   |        |
|----------|------------|--------|------------|---------------|---|--------|
| Source   | SS         | df     | MS         | Number of obs | = | 11,617 |
|          |            |        |            | F(4, 11612)   | = | 666.34 |
| Model    | 415.692168 | 4      | 103.923042 | Prob > F      | = | 0.0000 |
| Residual | 1811.03091 | 11,612 | .155962014 | R-squared     | = | 0.1867 |
|          |            |        |            | Adj R-squared | = | 0.1864 |
| Total    | 2226.72308 | 11,616 | .19169448  | Root MSE      | = | .39492 |

|               |             |           |        |       |                      |           |
|---------------|-------------|-----------|--------|-------|----------------------|-----------|
| chldlabour    | Coefficient | Std. err. | t      | P> t  | [95% conf. interval] |           |
| attending_now | -.3518561   | .0099296  | -35.44 | 0.000 | -.3713197            | -.3323925 |
| male          | .028782     | .0073294  | 3.93   | 0.000 | .0144152             | .0431488  |
| age           | .031503     | .001055   | 29.86  | 0.000 | .029435              | .033571   |
| pcincome      | -6.16e-09   | 4.77e-09  | -1.29  | 0.197 | -1.55e-08            | 3.19e-09  |
| _cons         | .1835022    | .016525   | 11.10  | 0.000 | .1511105             | .215894   |

- After controlling age, coefficient goes up -35.2
  - Bias term is negative:  $COV(\text{age}, \text{labour}) * COV(\text{age}, \text{schooling}) = (+) * (-)$
  - $-40.8 = -35.2 + \{ (+) * (-) \}$
  - $-40.8 = -35.2 + (-5.6)$

In the presence of omitted variable, estimated coefficient is

$$\widehat{\alpha}_1 = \beta_1 + \beta_2 * \widehat{\gamma}_1$$

|                               | Omitted variable (Z) | COV(Z,P)= $\gamma_1$ | COV(Z,Y)= $\beta_2$ | Direction of bias |
|-------------------------------|----------------------|----------------------|---------------------|-------------------|
| Y=earnings, P=training        |                      |                      |                     |                   |
| Y=health, P=insurance         |                      |                      |                     |                   |
| Y=harvest, P=HY seeds         |                      |                      |                     |                   |
| Y=weight, P=nutrition program |                      |                      |                     |                   |
| Y=revenue, P=obtained loan    |                      |                      |                     |                   |
| Y=IPV, P=yrs education        |                      |                      |                     |                   |

1) Modern applied economics is about counterfactual thinking

2) Identify the counterfactual

3) Is there selection bias?

4) Use toolkit to resolve the selection bias

Add relevant covariates (what do we mean by relevant?)

Study design (matching, discontinuity, randomization)

Econometrics (fixed-effects, DiD)