## NATIONAL BENCHMARKS

For State Achievement Standards


February 22, 2016

Gary W. Phillips
Vice President and Institute Fellow
American Institutes for Research

## Contents

Executive Summary ..... 1
Brief History of Common Core-Related Activities. ..... 3
Benchmarking State Achievement Standards ..... 5
Grades 4 and 8 Achievement Standards for Smarter Balanced, PARCC, ACT Aspire, and NAEP ..... 5
Using NAEP as a National Benchmark ..... 6
National NAEP Benchmarks for Smarter Balanced ..... 6
National NAEP Benchmarks for PARCC ..... 8
National NAEP Benchmarks for ACT Aspire ..... 9
National NAEP Benchmarks for Nonconsortium States ..... 11
Comparing Achievement Standards for Smarter Balanced, PARCC, and ACT Aspire ..... 16
Conclusion ..... 18
Caveats ..... 19
References ..... 21
Appendix: Methodology ..... 22
List of Tables
Table 1: Smarter Balanced Achievement Standards ..... 5
Table 2: PARCC Performance Standards ..... 6
Table 3: ACT Aspire Achievement Standards. ..... 6
Table 4: NAEP Achievement Standards ..... 6
Table 5: NAEP Equivalents of Smarter Balanced Achievement Standards for Level 2 ..... 7
Table 6: NAEP Equivalents of Smarter Balanced Achievement Standards for Level 3 ..... 7
Table 7: NAEP Equivalents of Smarter Balanced Achievement Standards for Level 4 ..... 8
Table 8: NAEP Equivalents of PARCC Performance Standards for Level 2 ..... 8
Table 9: NAEP Equivalents of PARCC Performance Standards for Level 3. ..... 9
Table 10: NAEP Equivalents of PARCC Performance Standards for Level 4. ..... 9
Table 11: NAEP Equivalents of PARCC Performance Standards for Level 5 ..... 9
Table 12: NAEP Equivalents of ACT Aspire Achievement Standards Level 2 ..... 10
Table 13: NAEP Equivalents of ACT Aspire Achievement Standards Level 3 ..... 10
Table 14: NAEP Equivalents of ACT Aspire Achievement Standards Level 4 ..... 11
Table 15: ELA Grade 4 NAEP Benchmarks for Nonconsortium States ..... 12
Table 16: ELA Grade 8 NAEP Benchmarks for Nonconsortium States ..... 13
Table 17: Mathematics Grade 4 NAEP Benchmarks for Nonconsortium States ..... 14
Table 18: Mathematics Grade 8 NAEP Benchmarks for Nonconsortium States ..... 15
Table 19: Smarter Balanced Versus PARCC. ..... 16
Table 20: Smarter Balanced Versus ACT Aspire ..... 17
Table 21: PARCC Versus ACT Aspire ..... 17

## Executive Summary

State achievement standards represent how much the state expects their students to learn in order to reach various levels of academic proficiency. In this study, the academic subjects are English language arts (ELA) and mathematics. In the past, these achievement standards were used by each state to report adequate yearly progress (AYP) under No Child Left Behind (NCLB) federal legislation, and they are currently being used for federal reporting under the Every Student Succeeds Act (ESSA) of 2015. These standards are also used by the state to monitor progress from year to year and to report on the success of each classroom, school, and district to parents and the public.

This report uses national benchmarking as a common metric to examine state achievement standards and compare how high these standards are compared to the National Assessment of Educational Progress (NAEP) achievement levels. It also compares how much students are expected to learn in some states with how much they are expected to learn in other states. The study uses NAEP grades 4 and 8 reading and mathematics as benchmarks for individual state achievement standards. The study also benchmarks the achievement standards of Smarter Balanced Assessment Consortium (referred to in this study as Smarter Balanced), Partnership for Assessment of Readiness for College and Careers (PARCC), and ACT Aspire. Benchmarking Smarter Balanced, PARCC, and ACT Aspire provides a common metric (i.e., the NAEP scale) that can be used to compare the stringency of their achievement standards. The most important findings in the study relate to achievement standards that represent college readiness. Each of these consortium tests in grades 4 and 8 has achievement standards that indicate the student is on track to be college ready. The college-ready standards are Level 3 (Met) for Smarter Balanced, Level 4 (Met) for PARCC, and Level 3 (Ready) for ACT Aspire.

The overall findings in the study are:

1. Smarter Balanced college-ready standards (Level 3) are comparable in difficulty to the NAEP Basic levels.
2. Smarter Balanced college-ready standards (Level 3) are significantly below PARCC college-ready standards (Level 4) by about one-quarter of a standard deviation. In the statistical literature, a standard deviation unit is referred to as an effect size. The effect sizes are for ELA grades 4 and 8, and mathematics grades 4 and 8 are $-.26,-.28,-.26$ and -.36 , respectively.
3. Smarter Balanced college-ready grade 8 standards are comparable to ACT Aspire college-ready grade 8 standards. However, for grade 4, the Smarter Balanced collegeready standard is significantly below the ACT Aspire college-ready standard for Reading (effect size $=-.26$ ) but significantly above the ACT Aspire college-ready standard for mathematics (effect size $=+.29$ ).
4. PARCC college-ready standards (Level 4) are comparable in difficulty to the NAEP Basic level for ELA and comparable to the NAEP Proficient level for mathematics.
5. PARCC college-ready standards (Level 4) are comparable in difficulty to the ACT Aspire college-ready standard for Reading grade 4. However, PARCC standards are significantly
above ACT Aspire college-ready standards for ELA grade 8 (effect size $=+.28$ ), mathematics grade 4 (effect size $=+.55$ ), and mathematics grade 8 (effect size $=+.48$ ).
6. ACT Aspire college-ready standards (Ready) are comparable in difficulty to the NAEP Basic levels.
7. Individual states that have college-readiness standards that map to the NAEP Proficient level are:
a. ELA grade 4-Florida and New York;
b. ELA grade 8-Florida, Kansas, and New York;
c. Mathematics grade 4-Florida and Kansas; and
d. Mathematics grade 8—Alaska, Florida, Kansas, New York, and Pennsylvania.

Note that Iowa, Nebraska, and Texas have three achievement levels, instead of the usual four levels or five levels in other states. At the time of this report, the author was unable to determine which levels in these states represented college readiness.

## Brief History of Common Core-Related Activities

Role of NCLB: Probably the biggest contributor to the development of the Common Core State Standards (CCSS) was the passage of the No Child Left Behind Act of 2001. A fundament problem with NCLB demonstrated the need for the CCSS. NCLB required each state to have challenging content standards and performance standards but left it up to the state to define what "challenging" meant. Some states used low standards in order to report higher levels of proficiency. States with low standards were living in a kind of Lake Wobegon world where more and more students were being reported as proficient but fewer and fewer students were prepared for college. This led the National Governors Association (NGA) and the Council of Chief State School Officers (CCSSO) to see if there was a way to make state standards more competitive and consistent.

Role of NGA and CCSSO: In 2006-2007, Arizona Governor Janet Napolitano chaired the NGA. In order to find a way to make America's educational system internationally competitive, she created a task force of state and national education policy leaders that released a report titled "Benchmarking for Success: Ensuring U.S. Students Receive a World-Class Education" (2008). The state leaders responsible for the report were the NGA and the CCSSO as well as the nonprofit group Achieve. The concepts in this report caught on, and in 2009 state leaders launched CCSS. These three groups obtained the support of other organizations that were critical in the development of the CCSS. These organizations included the American Federation of Teachers, the National Education Association, the National Council of Teachers of Mathematics, the National Council of Teachers of English, and the International Reading Association.

Role of U.S. Federal Government: The CCSS was a state-led effort and was not initiated by the federal government. The NGA and the CCSSO received no financial support from the federal government to develop the CCSS. However, once CCSS was developed, the federal government used the bully pulpit to encourage many states to implement internationally competitive common standards. For example, in 2009 President Obama, in a speech to the U.S. Hispanic Chamber of Commerce, recognized the need for high and consistent standards. He stated:

Let's challenge our states to adopt world-class standards that will bring our curriculums into the 21st century. Today's system of 50 different sets of benchmarks for academic success means fourth-grade readers in Mississippi are scoring nearly 70 points lower than students in Wyoming-and getting the same grade.

The federal government also provided seed money to help states implement common standards. The funding was provided in the 4.35 billion dollar Race to the Top grant as part of the American Recovery and Reinvestment Act of 2009, which was part of the federal economic stimulus package.

Role of Smarter Balanced and PARCC: Part of the Race to the Top grant was awarded to PARCC and Smarter Balanced to develop tests that measure the CCSS. Over several years of development, some states dropped out of the initiative. By spring 2015, 18 states had given the first operational administration of the Smarter Balanced assessment, and 11 states plus the District of Columbia gave the first operational administration of the PARCC assessment. These
are the jurisdictions on which the current consortium results are based. The Virgin Islands were also administered the Smarter Balanced assessment, but they were excluded in this mapping study because they did not participate in the 2015 NAEP assessment.

ACT Aspire: In 2015, ACT Aspire was administered in two states—Alabama and South Carolina-which represents a group of states taking the same assessment. Recognizing that a large portion of students were graduating high school unprepared for college, ACT developed an assessment that was built around college readiness beginning in elementary school. The ACT Aspire replaced the ACT Explore (grades 8 and 9) and ACT Plan (grade 10) and was administered in grades 3-10.

## Benchmarking State Achievement Standards

Benchmarking is a way to calibrate the difficulty level of state achievement standards so they can be compared to each other and to national standards. This type of benchmarking is similar to benchmarking in business and industry. For example, the fuel efficiency and quality of American-built cars are often benchmarked against those of cars built in Japan and South Korea. Such benchmarking is important in education if we are to expect our students to compete in a global economy. In this study, we use the NAEP as a national benchmark.

Some terminology clarification is needed in order to navigate through the results of this study. This report is about benchmarking (or comparing) state achievement standards (cut-scores on the state accountability test used to report results to the federal government under ESSA) to the NAEP achievement levels. In some testing programs, achievement standards are referred to as performance standards. The comparisons are obtained through equipercentile linking (described in the Appendix). An achievement standard is a specific number, or cut-score, on the scale such as those in Tables 1-3. What this study does is determine the NAEP equivalent of the state achievement standard (or cut-score) and report the NAEP achievement level in which the NAEP equivalent falls. For example, the Smarter Balanced ELA grade 4 cut-score for Level 3 is 2473 (see Table 1). The linking analysis shows this is equivalent in difficulty to a NAEP score of 222 (see Table 6). The NAEP equivalent of 222 falls within the range of the NAEP Basic level (208237; see Table 4).

## Grades 4 and 8 Achievement Standards for Smarter Balanced, PARCC, ACT Aspire, and NAEP

Each of the assessments used by groups of states in 2015 has its own achievement standards. In each case, the standards were set through a consortium or national consensus process and represent how much we expect students to know and be able to do at different levels of achievement. Possibly the most important achievement standard is the one that indicates the student is on track to be college ready by the end of high school. For Smarter Balanced this is Level 3, for PARCC this is Level 4, and for ACT Aspire this is Level 3. The achievement standards for each assessment-Smarter Balanced, PARCC, ACT Aspire, and NAEP—are indicated in Tables 1-4.

One caveat in the study is that for Smarter Balanced and PARCC we are mapping ELA standards, which include writing, to NAEP Reading standards, which do not include writing. This should not make much difference because, generally, the dis-attenuated correlations between reading and writing are very high.

Table 1: Smarter Balanced Achievement Standards

| Subject | Grade | Level 2 <br> Nearly Met | Level 3 <br> Met | Level 4 <br> Exceeded |
| :---: | :---: | :---: | :---: | :---: |
| ELA | 4 | 2416 | 2473 | 2533 |
| ELA | 8 | 2487 | 2567 | 2668 |
| Mathematics | 4 | 2411 | 2485 | 2549 |
| Mathematics | 8 | 2504 | 2586 | 2653 |

Table 2: PARCC Performance Standards

| Subject | Grade | Level 2 <br> Partially Met | Level 3 <br> Approached | Level 4 <br> Met | Level 5 <br> Exceeded |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ELA | 4 | 700 | 725 | 750 | 790 |
| ELA | 8 | 700 | 725 | 750 | 794 |
| Mathematics | 4 | 700 | 725 | 750 | 796 |
| Mathematics | 8 | 700 | 725 | 750 | 801 |

## Table 3: ACT Aspire Achievement Standards

| Subject | Grade | Level 2 <br> Close | Level 3 <br> Ready | Level 4 <br> Exceeding |
| :---: | :---: | :---: | :---: | :---: |
| Reading | 4 | 412 | 417 | 422 |
| Reading | 8 | 418 | 424 | 430 |
| Mathematics | 4 | 411 | 416 | 421 |
| Mathematics | 8 | 419 | 425 | 431 |

## Table 4: NAEP Achievement Standards

| Subject | Grade | Basic | Proficient | Advanced |
| :---: | :---: | :---: | :---: | :---: |
| Reading | 4 | 208 | 238 | 268 |
| Reading | 8 | 243 | 281 | 323 |
| Mathematics | 4 | 214 | 249 | 282 |
| Mathematics | 8 | 262 | 299 | 333 |

## Using NAEP as a National Benchmark

NAEP represents probably the best assessment against which to benchmark state achievement standards. First, the NAEP content standards and achievement standards were developed through an elaborate national process that has been exhaustively evaluated. NAEP standards have been demonstrated to be internationally competitive and are often referred to as the gold standard against which other standards can be compared. Second, NAEP provides biennial state representative assessments that can be treated as randomly equivalent to the local state testing population. This facilitates comparisons between local state testing results and state NAEP testing results. Third, because NAEP is administered in each state, the NAEP scale can be used as an anchor test to provide a common metric to compare local state-by-state testing results. This was the strategy used in this study.

## National NAEP Benchmarks for Smarter Balanced

In 2015, 18 states and the Virgin Islands administered the Smarter Balanced assessment. Because they all used the same test, a weighted average of the percentage at and above each achievement level for the 18 states was used for the analysis. The weights were based on the student
population size in each state. The 18 jurisdictions were California, Connecticut, Delaware, Hawaii, Idaho, Maine, Michigan, Missouri, Montana, Nevada, New Hampshire, North Dakota, Oregon, South Dakota, Vermont, Washington, West Virginia, and Wisconsin. The Virgin Islands were excluded because they did not participate in NAEP in 2015. For ELA, Wisconsin and Missouri were excluded from the weighted average because their administration deviated from the Smarter Balanced blueprint. North Dakota was excluded for both ELA and mathematics because the author was unable to find their results on their state web site. Aggregate NAEP estimates for the Smarter Balanced states were obtained from the NAEP Data Explorer (NDE).

The national NAEP benchmarks for Smarter Balanced are contained in Tables 5-7. The most important Smarter Balanced level to benchmark is Level 3, considered to represent being on track to be college ready. We see in Table 6 that each of the Smarter Balanced Level 3 cut-scores maps to the NAEP Basic achievement level.

Table 5: NAEP Equivalents of Smarter Balanced Achievement Standards for Level 2

| Subject | Grade | Smarter Cut- <br> Score for <br> Level 2 <br> Nearly Met | Percent at <br> and Above <br> Smarter <br> Level 2 <br> Nearly Met | NAEP Scaled <br> Score <br> Equivalent of <br> Level 2 <br> Nearly Met | Standard <br> Error of <br> NAEP <br> Equivalent of <br> Level 2 <br> Nearly Met | NAEP <br> Achievement <br> Level |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Equivalent of <br> Level 2 <br> Nearly Met |  |  |  |  |  |  |
| ELA | 4 | 2416 | 66 | 201 | 2.0 | Below Basic |
| ELA | 8 | 2487 | 77 | 236 | 1.0 | Below Basic |
| Math | 4 | 2411 | 74 | 216 | 1.0 | Basic |
| Math | 8 | 2504 | 61 | 269 | 1.0 | Basic |

Table 6: NAEP Equivalents of Smarter Balanced Achievement Standards for Level 3
$\left.\begin{array}{c|c|c|c|c|c|c}\text { Subject } & \text { Grade } & \begin{array}{c}\text { Smarter Cut- } \\ \text { Score for } \\ \text { Level 3 Met }\end{array} & \begin{array}{c}\text { Percent at } \\ \text { and Above } \\ \text { Smarter } \\ \text { Level 3 Met }\end{array} & \begin{array}{c}\text { NAEP Scaled } \\ \text { Score } \\ \text { Equivalent of } \\ \text { Level 3 Met }\end{array} & \begin{array}{c}\text { Standard } \\ \text { Error of } \\ \text { NAEP } \\ \text { Equivalent of } \\ \text { Level 3 Met }\end{array} & \begin{array}{c}\text { NAEP } \\ \text { Achievement } \\ \text { Level }\end{array} \\ \text { Equivalent of } \\ \text { Level 3 Met }\end{array}\right]$

Table 7: NAEP Equivalents of Smarter Balanced Achievement Standards for Level 4

| Subject | Grade | Smarter Cut- <br> Score for <br> Level 4 <br> Exceeded | Percent at <br> and Above <br> Smarter <br> Level 4 <br> Exceeded | NAEP Scaled <br> Score <br> Equivalent of <br> Level 4 <br> Exceeded | Standard <br> Error of <br> NAEP <br> Equivalent of <br> Level 4 <br> Exceeded | NAEP <br> Achievement <br> Level <br> Equivalent of <br> Level 4 <br> Exceeded |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ELA | 4 | 2533 | 22 | 247 | 2.0 | Proficient |
| ELA | 8 | 2668 | 13 | 302 | 1.0 | Proficient |
| Math | 4 | 2549 | 15 | 268 | 1.0 | Proficient |
| Math | 8 | 2653 | 17 | 315 | 1.0 | Proficient |

## National NAEP Benchmarks for PARCC

In 2015, 11 states and the District of Columbia administered the PARCC assessment. Because they all used the same test, a weighted average of the percentage at and above each achievement level for the 12 jurisdictions was used for the analysis. The weights were based on the student population size in each state. The 12 jurisdictions were Arkansas, Colorado, District of Columbia, Illinois, Louisiana, Maryland, Massachusetts, Mississippi, New Jersey, New Mexico, Ohio, and Rhode Island. The aggregate NAEP estimate for the PARCC jurisdictions was obtained from the NDE.

The national NAEP benchmarks for PARCC are contained in Tables $8-11$. The most important PARCC level to benchmark is Level 4, considered to represent being on track to be college ready. We see in Table 10 that each of the PARCC Level 4 cut-scores maps to the NAEP Basic achievement level for ELA and the NAEP Proficient achievement level for mathematics.

Table 8: NAEP Equivalents of PARCC Performance Standards for Level 2

| Subject | Grade | PARCC Cut- <br> Score for <br> Level 2 <br> Partially Met | Percent at <br> and Above <br> PARCC <br> Level 2 <br> Partially Met | NAEP Scaled <br> Score <br> Equivalent of <br> Level 2 <br> Partially Met | Standard <br> Error of <br> NAEP <br> Equivalent of <br> Level 2 <br> Partially Met | NAEP <br> Achievement <br> Level <br> Equivalent of <br> Level 2 <br> Partially Met |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ELA | 4 | 700 | 89 | 179 | 1.0 | Below Basic |
| ELA | 8 | 700 | 86 | 229 | 1.0 | Below Basic |
| Math | 4 | 700 | 88 | 200 | 1.0 | Below Basic |
| Math | 8 | 700 | 78 | 255 | 1.0 | Below Basic |

Table 9: NAEP Equivalents of PARCC Performance Standards for Level 3

| Subject | Grade | PARCC Cut- <br> Score for <br> Level 3 <br> Approached | Percent at <br> and Above <br> PARCC <br> Level 3 <br> Approached | NAEP Scaled <br> Score <br> Equivalent of <br> Level 3 <br> Approached | Standard <br> Error of <br> NAEP <br> Equivalent of <br> Level 3 <br> Approached | NAEP <br> Achievement <br> Level |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Equivalent of <br> Level 3 <br> Approached |  |  |  |  |  |  |
| ELA | 4 | 725 | 70 | 205 | 1.0 | Below Basic |
| ELA | 8 | 725 | 67 | 250 | 1.0 | Basic |
| Math | 4 | 725 | 62 | 228 | 1.0 | Basic |
| Math | 8 | 725 | 52 | 282 | 1.0 | Basic |

Table 10: NAEP Equivalents of PARCC Performance Standards for Level 4

| Subject | Grade | PARCC Cut- <br> Score for <br> Level 4 Met | Percent at <br> and Above <br> PARCC <br> Level 4 Met | NAEP Scaled <br> Score <br> Equivalent of <br> Level 4 Met | Standard <br> Error of <br> NAEP <br> Equivalent of <br> Level 4 Met | NAEP <br> Achievement <br> Level |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Equivalent of |  |  |  |  |  |  |
| Level 4 Met |  |  |  |  |  |  |

Table 11: NAEP Equivalents of PARCC Performance Standards for Level 5

| Subject | Grade | PARCC Cut- <br> Score for <br> Level 5 <br> Exceeded | Percent at <br> and Above <br> PARCC <br> Level 5 <br> Exceeded | NAEP Scaled <br> Score <br> Equivalent of <br> Level 5 <br> Exceeded | Standard <br> Error of <br> NAEP <br> Equivalent of <br> Level 5 <br> Exceeded | NAEP <br> Achievement <br> Level |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Equivalent of <br> Level 5 <br> Exceeded |  |  |  |  |  |  |
| ELA | 4 | 790 | 7 | 277 | 1.0 | Advanced |
| ELA | 8 | 794 | 7 | 318 | 1.0 | Proficient |
| Math | 4 | 796 | 3 | 297 | 2.0 | Advanced |
| Math | 8 | 801 | 3 | 358 | 1.0 | Advanced |

## National NAEP Benchmarks for ACT Aspire

In 2015, two states administered the ACT Aspire test. They were Alabama and South Carolina. Because both states used the same test, a weighted average of the percentage at and above each
achievement level was used for the analysis. The weights were based on the student population size in each state. The aggregate NAEP estimate for the ACT Aspire jurisdictions was obtained from the NDE. The national NAEP benchmarks for ACT Aspire are contained in Tables 12-14. The most important ACT Aspire level to benchmark is Level 3, considered to represent being on track to be college ready. We see in Table 13 that each of the ACT Aspire college-ready cutscores map to the NAEP Basic achievement level.

Table 12: NAEP Equivalents of ACT Aspire Achievement Standards Level 2

| Subject | Grade | ACT Aspire <br> Cut-Score for <br> Level 2 Close | Percent at <br> and Above <br> ACT Aspire <br> Level 2 Close | NAEP Scaled <br> Score <br> Equivalent of <br> Level 2 Close | Standard <br> Error of <br> NAEP <br> Equivalent of <br> Level 2 Close | NAEP <br> Achievement <br> Level <br> Equivalent of <br> Level 2 Close |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Reading | 4 | 412 | 67 | 202 | 2.0 | Below Basic |
| Reading | 8 | 418 | 72 | 240 | 1.0 | Below Basic |
| Math | 4 | 411 | 91 | 195 | 1.0 | Below Basic |
| Math | 8 | 419 | 59 | 263 | 2.0 | Basic |

Table 13: NAEP Equivalents of ACT Aspire Achievement Standards Level 3

| Subject | Grade | ACT Aspire <br> Cut-Score for <br> Level 3 <br> Ready | Percent at <br> and Above <br> ACT Aspire <br> Level 3 <br> Ready | NAEP Scaled <br> Score <br> Equivalent of <br> Level 3 <br> Ready | Standard <br> Error of <br> NAEP <br> Equivalent of <br> Level 3 <br> Ready | NAEP <br> Achievement <br> Level |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Equivalent of |  |  |  |  |  |  |
| Level 3 |  |  |  |  |  |  |
| Ready |  |  |  |  |  |  |

Table 14: NAEP Equivalents of ACT Aspire Achievement Standards Level 4

| Subject | Grade | ACT Aspire <br> Cut-Score <br> for Level 4 <br> Exceeding | Percent at <br> and Above <br> ACT Aspire <br> Level 4 <br> Exceeding | NAEP <br> Scaled Score <br> Equivalent <br> of Level 4 <br> Exceeding | Standard <br> Error of <br> NAEP <br> Equivalent <br> of Level 4 <br> Exceeding | NAEP <br> Achievement <br> Level <br> Equivalent <br> of Level 4 <br> Exceeding |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Reading | 4 | 422 | 13 | 260 | 2.0 | Proficient |
| Reading | 8 | 430 | 13 | 298 | 2.0 | Proficient |
| Math | 4 | 421 | 14 | 266 | 1.0 | Proficient |
| Math | 8 | 431 | 14 | 309 | 2.0 | Proficient |

## National NAEP Benchmarks for Nonconsortium States

Across most of the nonconsortium states with four achievement levels, Level 3 is considered on track to be college ready. For many states with five achievement levels, Level 4 is considered on track to be college ready. However, this is not universally true. For Indiana, the author was not able to obtain the 2015 state results at the present time.

The results of NAEP benchmarks for ELA grade 4 individual states are reported in Table 15. The reading grade 4 NAEP achievement level cut-scores are Basic $=208$, Proficient $=238$, and Advanced $=268$. The only state with four achievement levels for which Level 3 maps to the NAEP Proficient level is New York. The only state with five achievement levels for which Level 4 maps to the NAEP Proficient level is Florida.

Table 15：ELA Grade 4 NAEP Benchmarks for Nonconsortium States

| State | ELA Grade 4 |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Level 2 |  |  | Level 3 |  |  | Level 4 |  |  | Level 5 |  |  |
|  |  | 首 | $\begin{aligned} & \text { NAEP Achievement Level } \\ & \text { Comparable to Level } 2 \end{aligned}$ |  |  | 范 |  | 光 |  |  | 兑 |  |
| Alaska | 59 | 203 | Below <br> Basic | 40 | 224 | Basic | 9 | 271 | Advanced |  |  |  |
| Arizona | 59 | 206 | Below Basic | 42 | 223 | Basic | 6 | 277 | Advanced |  |  |  |
| DoDEA | 93 | 193 | Below Basic | 72 | 217 | Basic | 37 | 243 | Proficient |  |  |  |
| Florida | 79 | 202 | Below Basic | 54 | 224 | Basic | 27 | 246 | Proficient | 8 | 271 | Advanced |
| Georgia | 71 | 204 | Below Basic | 37 | 233 | Basic | 9 | 267 | Proficient |  |  |  |
| Iowa | 76 | 198 | Below <br> Basic | 29 | 244 | Proficient |  |  |  |  |  |  |
| Kansas | 88 | 176 | Below <br> Basic | 55 | 217 | Basic | 11 | 269 | Advanced |  |  |  |
| Kentucky | 81 | 199 | Below Basic | 52 | 226 | Basic | 14 | 263 | Proficient |  |  |  |
| Minnesota | 79 | 192 | Below Basic | 58 | 216 | Basic | 18 | 259 | Proficient |  |  |  |
| Nebraska | 81 | 196 | Below Basic | 38 | 237 | Basic |  |  |  |  |  |  |
| New York | 68 | 206 | Below Basic | 32 | 240 | Proficient | 11 | 267 | Proficient |  |  |  |
| North Carolina | 77 | 201 | Below Basic | 59 | 218 | Basic | 47 | 228 | Basic | 7 | 275 | Advanced |
| Oklahoma | 85 | 188 | Below Basic | 70 | 205 | Below Basic | 4 | 279 | Advanced |  |  |  |
| Pennsylvania | 87 | 185 | Below Basic | 59 | 219 | Basic | 22 | 255 | Proficient |  |  |  |
| Tennessee | 88 | 172 | Below Basic | 45 | 224 | Basic | 14 | 261 | Proficient |  |  |  |
| Texas | 74 | 194 | Below Basic | 21 | 247 | Proficient |  |  |  |  |  |  |
| Utah | 69 | 208 | Basic | 42 | 233 | Basic | 13 | 267 | Proficient |  |  |  |
| Virginia | 97 | 160 | Below Basic | 77 | 202 | Below Basic | 20 | 260 | Proficient |  |  |  |
| Wyoming | 85 | 195 | Below Basic | 61 | 219 | Basic | 18 | 259 | Proficient |  |  |  |

The results of NAEP benchmarks for ELA grade 8 individual states are reported in Table 16. The reading grade 8 NAEP achievement level cut-scores are Basic $=243$, Proficient $=281$, and Advanced $=323$. The states with four achievement levels for which Level 3 maps to the NAEP Proficient level are Kansas and New York. The only state with five achievement levels for which Level 4 maps to the NAEP Proficient level is Florida.

Table 16: ELA Grade 8 NAEP Benchmarks for Nonconsortium States

| State | ELA Grade 8 |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Level 2 |  |  | Level 3 |  |  | Level 4 |  |  | Level 5 |  |  |
|  |  | 苞 |  |  |  |  |  |  |  | ص |  |  |
| Alaska | 80 | 228 | Below <br> Basic | 31 | 279 | Basic | 2 | 337 | Advanced |  |  |  |
| Arizona | 61 | 253 | Basic | 35 | 276 | Basic | 8 | 311 | Proficient |  |  |  |
| DoDEA | 96 | 230 | Below Basic | 79 | 256 | Basic | 41 | 283 | Proficient |  |  |  |
| Florida | 78 | 239 | Below <br> Basic | 55 | 259 | Basic | 29 | 281 | Proficient | 11 | 303 | Proficient |
| Georgia | 76 | 238 | Below Basic | 39 | 272 | Basic | 8 | 312 | Proficient |  |  |  |
| Iowa | 75 | 246 | Basic | 24 | 291 | Proficient |  |  |  |  |  |  |
| Kansas | 78 | 241 | Below <br> Basic | 29 | 285 | Proficient | 2 | 333 | Advanced |  |  |  |
| Kentucky | 79 | 241 | Below <br> Basic | 54 | 264 | Basic | 18 | 299 | Proficient |  |  |  |
| Minnesota | 75 | 248 | Basic | 56 | 265 | Basic | 20 | 299 | Proficient |  |  |  |
| Nebraska | 79 | 244 | Basic | 36 | 281 | Basic |  |  |  |  |  |  |
| New York | 60 | 254 | Basic | 22 | 291 | Proficient | 7 | 317 | Proficient |  |  |  |
| North Carolina | 79 | 231 | Below Basic | 53 | 257 | Basic | 42 | 269 | Basic | 10 | 309 | Proficient |
| Oklahoma | 87 | 226 | Below Basic | 75 | 241 | Below Basic | 16 | 295 | Proficient |  |  |  |
| Pennsylvania | 89 | 225 | Below Basic | 58 | 262 | Basic | 15 | 306 | Proficient |  |  |  |
| Tennessee | 91 | 221 | Below Basic | 50 | 265 | Basic | 11 | 306 | Proficient |  |  |  |
| Texas | 78 | 234 | Below <br> Basic | 23 | 286 | Proficient |  |  |  |  |  |  |
| Utah | 66 | 256 | Basic | 42 | 276 | Basic | 15 | 304 | Proficient |  |  |  |
| Virginia | 96 | 207 | Below Basic | 75 | 244 | Basic | 11 | 309 | Proficient |  |  |  |
| Wyoming | 79 | 244 | Basic | 52 | 268 | Basic | 12 | 305 | Proficient |  |  |  |

The results of NAEP benchmarks for mathematics grade 4 individual states are reported in Table 17．The mathematics grade 4 NAEP achievement level cut－scores are Basic $=214$ ， Proficient $=249$ ，and Advanced $=282$ ．The only state with four achievement levels for which Level 3 maps to the NAEP Proficient level is Kansas．The only state with five achievement levels for which Level 4 maps to the NAEP Proficient level is Florida．

Table 17：Mathematics Grade 4 NAEP Benchmarks for Nonconsortium States

| State | Mathematics Grade 4 |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Level 2 |  |  | Level 3 |  |  | Level 4 |  |  | Level 5 |  |  |
|  |  |  | 范 |  | 毛 |  | 若 |  | 苋 |  |  |  |
| Alaska | 86 | 202 | Below <br> Basic | 39 | 245 | Basic | 8 | 279 | Proficient |  |  |  |
| Arizona | 72 | 220 | Basic | 42 | 244 | Basic | 10 | 276 | Proficient |  |  |  |
| DoDEA | 88 | 218 | Basic | 66 | 237 | Basic | 39 | 255 | Proficient |  |  |  |
| Florida | 77 | 222 | Basic | 59 | 236 | Basic | 31 | 256 | Proficient | 12 | 275 | Proficient |
| Georgia | 80 | 212 | Below <br> Basic | 40 | 244 | Basic | 9 | 275 | Proficient |  |  |  |
| Iowa | 79 | 219 | Basic | 29 | 260 | Proficient |  |  |  |  |  |  |
| Kansas | 85 | 211 | Below <br> Basic | 35 | 252 | Proficient | 8 | 282 | Advanced |  |  |  |
| Kentucky | 80 | 219 | Basic | 49 | 243 | Basic | 16 | 270 | Proficient |  |  |  |
| Minnesota | 85 | 217 | Basic | 70 | 233 | Basic | 36 | 261 | Proficient |  |  |  |
| Nebraska | 77 | 223 | Basic | 24 | 263 | Proficient |  |  |  |  |  |  |
| New York | 73 | 219 | Basic | 43 | 242 | Basic | 19 | 262 | Proficient |  |  |  |
| North Carolina | 79 | 221 | Basic | 56 | 239 | Basic | 49 | 245 | Basic | 18 | 270 | Proficient |
| Oklahoma | 90 | 206 | Below <br> Basic | 72 | 224 | Basic | 27 | 256 | Proficient |  |  |  |
| Pennsylvania | 75 | 222 | Basic | 44 | 248 | Basic | 17 | 273 | Proficient |  |  |  |
| Tennessee | 85 | 211 | Below <br> Basic | 50 | 240 | Basic | 21 | 264 | Proficient |  |  |  |
| Texas | 73 | 227 | Basic | 17 | 271 | Proficient |  |  |  |  |  |  |
| Utah | 71 | 226 | Basic | 51 | 242 | Basic | 26 | 261 | Proficient |  |  |  |
| Virginia | 97 | 193 | Below <br> Basic | 84 | 218 | Basic | 28 | 263 | Proficient |  |  |  |
| Wyoming | 88 | 214 | Basic | 51 | 246 | Basic | 13 | 278 | Proficient |  |  |  |

The results of NAEP benchmarks for mathematics grade 8 individual states are reported in Table 18．The mathematics grade 8 NAEP achievement level cut－scores are Basic＝262， Proficient $=299$ ，and Advanced $=333$ ．The only states with four achievement levels for which Level 3 maps to the NAEP Proficient level are Alaska，Kansas，New York，and Pennsylvania． The only state with five achievement levels for which Level 4 maps to the NAEP Proficient level is Florida．

In some states，some of the grade 8 students took the Algebra 1 test．In this benchmarking study， this factor could have had the effect of making the grade 8 mathematics standards appear higher．

Table 18：Mathematics Grade 8 NAEP Benchmarks for Nonconsortium States

| State | Mathematics Grade 8 |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Level 2 |  |  | Level 3 |  |  | Level 4 |  |  | Level 5 |  |  |
|  |  | 首 | 葛 |  |  | 苋 |  | 首 |  |  | 药 | ח10 |
| Alaska | 89 | 236 | Below Basic | 26 | 304 | Proficient | 1 | 361 | Advanced |  |  |  |
| Arizona | 59 | 275 | Basic | 34 | 298 | Basic | 14 | 323 | Proficient |  |  |  |
| DoDEA | 96 | 236 | Below Basic | 78 | 267 | Basic | 45 | 295 | Basic |  |  |  |
| Florida | 71 | 256 | Below Basic | 45 | 280 | Basic | 18 | 308 | Proficient | 7 | 328 | Proficient |
| Georgia | 75 | 254 | Below Basic | 37 | 291 | Basic | 12 | 321 | Proficient |  |  |  |
| Iowa | 75 | 262 | Below Basic | 24 | 312 | Proficient |  |  |  |  |  |  |
| Kansas | 62 | 274 | Basic | 22 | 309 | Proficient | 4 | 344 | Advanced |  |  |  |
| Kentucky | 85 | 242 | Below Basic | 44 | 283 | Basic | 11 | 320 | Proficient |  |  |  |
| Minnesota | 80 | 264 | Basic | 58 | 287 | Basic | 27 | 317 | Proficient |  |  |  |
| Nebraska | 68 | 270 | Basic | 22 | 313 | Proficient |  |  |  |  |  |  |
| New York | 60 | 271 | Basic | 22 | 308 | Proficient | 7 | 334 | Advanced |  |  |  |
| North Carolina | 70 | 262 | Below Basic | 43 | 288 | Basic | 36 | 295 | Basic | 11 | 328 | Proficient |
| Oklahoma | 79 | 248 | Below Basic | 53 | 272 | Basic | 11 | 314 | Proficient |  |  |  |
| Pennsylvania | 62 | 271 | Basic | 30 | 304 | Proficient | 8 | 338 | Advanced |  |  |  |
| Tennessee | 81 | 246 | Below Basic | 54 | 274 | Basic | 29 | 299 | Basic |  |  |  |
| Texas | 75 | 261 | Below Basic | 6 | 336 | Advanced |  |  |  |  |  |  |
| Utah | 70 | 267 | Basic | 41 | 294 | Basic | 14 | 325 | Proficient |  |  |  |
| Virginia | 93 | 235 | Below Basic | 74 | 265 | Basic | 9 | 336 | Advanced |  |  |  |
| Wyoming | 84 | 255 | Below Basic | 47 | 289 | Basic | 10 | 327 | Proficient |  |  |  |

## Comparing Achievement Standards for Smarter Balanced，PARCC， and ACT Aspire

One of the advantages of mapping state achievement standards to NAEP is that the NAEP scale can serve as a common metric with which to compare the achievement standards of Smarter Balanced，PARCC，and ACT Aspire．The strategy is to obtain the NAEP equivalent of each consortium achievement standard and then compare their NAEP equivalents．The procedure used in this report is to compare their NAEP equivalents by using a two－tailed $Z$ test with $p<.05$ ．The standard error used in the $Z$ test is described in the Appendix．

The most important comparisons are between the college－ready standards of the group assessments．Comparing Smarter Balanced versus PARCC in Table 19 we find that

1．Smarter Balanced college－ready standards（Level 3）are comparable in difficulty to the NAEP Basic levels，and

2．Smarter Balanced college－ready standards（Level 3）are significantly below PARCC college－ready standards（Level 4）by about one－quarter of a standard deviation．

Table 19：Smarter Balanced Versus PARCC

|  |  | Smarter Balanced |  |  | PARCC |  |  | Difference |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \stackrel{\rightharpoonup}{\nu} \\ & \stackrel{\rightharpoonup}{\bar{\omega}} \end{aligned}$ | $\begin{aligned} & \text { تِّ } \\ & \cline { 1 - 2 } \end{aligned}$ |  |  | 岂 |  |  | 导 |  |  |
| ELA | 4 | 222 | 2 | Basic | 232 | 1 | Basic | YES | －． 26 |
| ELA | 8 | 264 | 1 | Basic | 273 | 1 | Basic | YES | －． 28 |
| Math | 4 | 244 | 1 | Basic | 252 | 1 | Proficient | YES | －． 26 |
| Math | 8 | 294 | 1 | Basic | 307 | 1 | Proficient | YES | －． 36 |

We can also compare the achievement standards of Smarter Balanced to those of ACT Aspire． When we compare the college－ready standards in Table 20，we find that

1．both Smarter Balanced and ACT Aspire college－ready standards（Ready）are comparable in difficulty to the NAEP Basic level；and
2．Smarter Balanced college－ready grade 8 standards are statistically comparable to ACT Aspire college－ready grade 8 standards．However，for grade 4，the Smarter Balanced college－ready standard is significantly below the ACT Aspire college－ready standard for ELA and reading（effect size $=-.26$ ）but significantly above the ACT Aspire college－ ready standard for mathematics（effect size＝＋．29）．

Table 20：Smarter Balanced Versus ACT Aspire

|  |  | Smarter Balanced |  |  | ACT Aspire |  |  | Difference |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 首 |  | 岂 |  |  | 势 |  |  |
| ELA／ <br> Reading | 4 | 222 | 2 | Basic | 232 | 2 | Basic | YES | －． 26 |
| ELA／ <br> Reading | 8 | 264 | 1 | Basic | 264 | 1 | Basic | NO |  |
| Math | 4 | 244 | 1 | Basic | 235 | 1 | Basic | YES | ． 29 |
| Math | 8 | 294 | 1 | Basic | 290 | 2 | Basic | NO |  |

Similarly，we can compare PARCC and ACT Aspire college－ready standards．From Table 21， PARCC college－ready standards（Level 4）are statistically comparable in difficulty to the ACT Aspire college－ready standard for ELA and reading grade 4．However，PARCC standards are significantly above ACT Aspire college－ready standards for ELA and reading grade 8 （effect size $=+.28$ ），mathematics grade 4 （effect size $=+.55$ ），and mathematics grade 8 （effect size $=+.48$ ）．

Table 21：PARCC Versus ACT Aspire

|  |  | PARCC |  |  | ACT Aspire |  |  | Difference |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | 范 |  | 导 |  |  |
| ELA／ <br> Reading | 4 | 232 | 1 | Basic | 232 | 2 | Basic | NO |  |
| ELA／ <br> Reading | 8 | 273 | 1 | Basic | 264 | 1 | Basic | YES | ． 28 |
| Math | 4 | 252 | 1 | Proficient | 235 | 1 | Basic | YES | ． 55 |
| Math | 8 | 307 | 1 | Proficient | 290 | 2 | Basic | YES | ． 48 |

## Conclusion

There are essentially three overall findings in this study.

1. A handful of nonconsortium states have college-ready standards that are at least as stringent as the NAEP Proficient level. These are
a. ELA grade 4-Florida and New York;
b. ELA grade 8-Florida, Kansas, and New York;
c. Mathematics grade 4—Florida and Kansas; and
d. Mathematics grade 8—Alaska, Florida, Kansas, New York, and Pennsylvania.
2. For the group-based assessments, only PARCC mathematics, grades 4 and 8 , have college-ready standards comparable in difficulty to the NAEP Proficient level.
3. The Smarter Balanced achievement standards are about one-quarter of a standard deviation lower than the PARCC performance standards.

The benchmarking study reported here should give policy makers insight into what states are expecting from their students. Some states expect more, and some expect less. The study is intended to provide a way to benchmark and compare state achievement standards and benchmark and compare the achievement standards of Smarter Balanced, PARCC, and ACT Aspire. The study does not intend to evaluate state achievement standards or make policy recommendations.

## Caveats

There are several caveats that are important to note in this study. First, the results in this report do not provide final and complete information about each state. The author was unable to obtain the results for several states, and some states have reported their results as preliminary. In the future, the National Center for Education Statistics (NCES) will conduct their biennial state mapping study. By that time, the NCES should be able to provide a more definitive and comprehensive mapping study.

Second, in some states, some of the grade 8 mathematics students took an end-of-course test, such as Algebra 1. In this benchmarking study, this factor could have had the effect of making the state grade 8 mathematics standards appear higher.

Third, this study maps state achievement standards to NAEP achievement levels and highlights those state standards that reach the NAEP Proficient level. This should not be interpreted to mean that NAEP's Proficient levels in grades 4 and 8 are the gold standards for deciding whether our students are on track to be ready for college. No evidence has been presented by NAEP that the proficient standard in grades 4 and 8 predicts college success. It is the case that NAEP used $12^{\text {th }}$ grade college-ready cut-scores (2013) to report that about $38 \%$ of students have the reading skills, and $39 \%$ have the math skills that make them ready for college. The cut-scores were 302 for reading and 163 for mathematics. The reading college-ready cut-score was equal to the reading proficient standard, and the mathematics cut-score was just below the mathematics proficient standard.

Fourth, there are some interpretive nuances related to the methodology used in this study. This report uses statistical linking to map state achievement standards onto the NAEP scale. Holland (2007) has outlined three broad categories of linking. These are equating, scale alignment, and prediction. A fundamental difference among the three methods is related to the degree to which they assume the two tests measure the same content and have the same administrative procedures.

- In equating, both tests must be constructed to measure the same identical content, be equally reliable, and both tests must use the same administrative procedures.
- In scale alignment, both tests measure similar but not identical content, may not be equally reliable, and there can be variation in administrative procedures. Scale alignment can provide a good ballpark estimate of how scores line up, but is less precise than equating.
- In prediction, there are no assumptions at all about content, reliability or administrative procedures.

This report uses the second type: scale alignment. The scales we are aligning will not measure identical constructs ${ }^{1}$, will not be equally reliable, and will not use identical administrative

[^0]procedures. The method of alignment is equiprecentile linking based on the aggregate reporting of NAEP and the state assessments. It is the scales of the total aggregate distributions that are aligned, so the linking should not be used for disaggregated reporting of individual students or demographic subgroups (such as race/ethnicity or gender) or subpopulations (such as schools). Also, the reader should be aware that the concordance between NAEP and the state assessments established in this report for 2015 may not be applicable in subsequent years.

Fifth, this report does not, in any way, address or evaluate the quality of the CCSS. The CCSS are content standards, while this report deals only with achievement standards. Content standards represent the curriculum that teachers should teach, and the scope and sequence of what students should learn in school. Achievement standards are cut-scores on the state test that represent performance expectations. For example, what level of performance on the test do we think represents being on track to be college ready.

## References

Daro, P., Hughes, G. B., and Stancavage, F. (2015). Study of the Alignment of the 2015 NAEP Mathematics Items at Grade 4 and 8 to the Common Core State Standards (CCSS) for Mathematics. (see http://www.air.org/project/naep-validity-studies-nvs-panel)

Holland, P. W. (2007). A framework and history for score linking. In N. J. Dorans, M. Pommerich, \& P. W. Holland (Eds.), Linking and aligning scores and scales, New York, NY: Springer.

National Governors Association, Council of Chief State School Officers, Achieve. (2008). Benchmarking for success: Ensuring U.S. students receive a world-class education. Washington, DC: National Governors Association.

NAEP as an Indicator of Students’ Academic Preparedness for College. U.S. Department of Education, Institute of Education Sciences, National Center for Education Statistics, National Assessment of Educational Progress (NAEP), 2013 Mathematics and Reading Assessments.

No Child Left Behind Act of 2001, Pub. L. No. 107-110, § 115, Stat. 1425 (2002).
Obama, B. (2009, March 10). President Obama’s remarks to the Hispanic Chamber of Commerce. New York Times.

## Appendix: Methodology

This study uses equipercentile linking to benchmark state achievement standards against NAEP achievement levels. The derivations described below make two assumptions. First, we assume the state test scores and the NAEP test scores are normal distributions. Second, we assume the NAEP examinee sample is randomly equivalent to the population of examinees who took the state test.

NAEP scores are assumed to have a normal distribution $N\left(\hat{\mu}_{N}, \hat{\sigma}_{N}^{2}\right)$, where the standard error of $\hat{\mu}_{N}$ is estimated by $\hat{\sigma}_{\widehat{\mu}_{N}}$, the standard error of $\hat{\sigma}_{N}$ is $\hat{\sigma}_{\widehat{\sigma}_{N}}$, and the covariance between $\hat{\mu}_{N}$ and $\hat{\sigma}_{N}$ is $\hat{\sigma}_{\widehat{\mu}_{N}, \widehat{\sigma}_{N}}$, usually 0 if from a normal sample.

If the state-level proportion at and above the cut $c$ is $\hat{p}_{c}$ with standard error of $\hat{\sigma}_{\hat{p}_{c}}$, the corresponding NAEP equivalent score, $\hat{s}_{N}$ assuming random equivalent group tests, can be estimated by solving the equation

$$
1-\hat{p}_{c}=\int_{-\infty}^{\hat{s}_{N}} \frac{\operatorname{Exp}\left(-\frac{\left(x-\hat{\mu}_{N}\right)^{2}}{2 \hat{\sigma}_{N}^{2}}\right)}{\sqrt{2 \pi} \hat{\sigma}_{N}} d x
$$

Let $y=\frac{x-\widehat{\mu}_{N}}{\widehat{\sigma}_{N}}$, and making the change of variable, we obtain

$$
1-\hat{p}_{c}=\int_{-\infty}^{\frac{\hat{s}_{N}-\widehat{\mu}_{N}}{\widehat{\sigma}_{N}}} \frac{\operatorname{Exp}\left(-\frac{y^{2}}{2}\right)}{\sqrt{2 \pi}} d y
$$

or

$$
\frac{\hat{s}_{N}-\hat{\mu}_{N}}{\hat{\sigma}_{N}}=\Phi^{-1}\left(1-\hat{p}_{c}\right) .
$$

So

$$
\hat{s}_{N}=\hat{\mu}_{N}+\hat{\sigma}_{N} \Phi^{-1}\left(1-\hat{p}_{c}\right) .
$$

Using delta method, the variance of the NAEP equivalent score $\hat{s}_{N}$ can be estimated by

$$
\begin{aligned}
\operatorname{Var}\left(\hat{s}_{N}\right)= & \operatorname{Var}\left(\hat{\mu}_{N}\right)+2 \Phi^{-1}\left(1-\hat{p}_{c}\right) \operatorname{Cov}\left(\hat{\mu}_{N}, \hat{\sigma}_{N}\right)+\operatorname{Var}\left(\hat{\sigma}_{N}\right)\left(\Phi^{-1}\left(1-\hat{p}_{c}\right)\right)^{2} \\
& +\hat{\sigma}_{N}^{2} \operatorname{Var}\left(\Phi^{-1}\left(1-\hat{p}_{c}\right)\right),
\end{aligned}
$$

or

$$
\operatorname{Var}\left(\hat{s}_{N}\right)=\hat{\sigma}_{\widehat{\mu}_{N}}^{2}+2 \Phi^{-1}\left(1-\hat{p}_{c}\right) \hat{\sigma}_{\hat{\mu}_{N}, \widehat{\sigma}_{N}}+\left(\Phi^{-1}\left(1-\hat{p}_{c}\right)\right)^{2} \hat{\sigma}_{\widehat{\sigma}_{N}}^{2}+\hat{\sigma}_{N}^{2}\left(\varphi\left(\Phi^{-1}\left(1-\hat{p}_{c}\right)\right)\right)^{-2} \hat{\sigma}_{\hat{p}_{c}}^{2} .
$$

The standard error of the NAEP equivalent score $\hat{s}_{N}$ is then estimated by

$$
\hat{\sigma}_{\hat{S}_{N}}=\sqrt{\hat{\sigma}_{\hat{\mu}_{N}}^{2}+2 \Phi^{-1}\left(1-\hat{p}_{c}\right) \hat{\sigma}_{\hat{\mu}_{N}, \widehat{\sigma}_{N}}+\left(\Phi^{-1}\left(1-\hat{p}_{c}\right)\right)^{2} \hat{\sigma}_{\widehat{\sigma}_{N}}^{2}+\hat{\sigma}_{N}^{2}\left(\varphi\left(\Phi^{-1}\left(1-\hat{p}_{c}\right)\right)\right)^{-2} \hat{\sigma}_{\hat{p}_{c}}^{2}}
$$

where $\Phi$ is the cumulative distribution function of the standard normal distribution and $\varphi$ is the probability density function of the standard normal distribution. Assuming $\operatorname{Cov}\left(\hat{\mu}_{N}, \hat{\sigma}_{N}\right)=0$, this is simplified to

$$
\hat{\sigma}_{\hat{s}_{N}}=\sqrt{\hat{\sigma}_{\widehat{\mu}_{N}}^{2}+\left(\Phi^{-1}\left(1-\hat{p}_{c}\right)\right)^{2} \hat{\sigma}_{\hat{\sigma}_{N}}^{2}+\hat{\sigma}_{N}^{2}\left(\varphi\left(\Phi^{-1}\left(1-\hat{p}_{c}\right)\right)\right)^{-2} \hat{\sigma}_{\hat{p}_{c}}^{2}}
$$

The values of $\hat{\sigma}_{\hat{S}_{N}}$ were rounded up to the nearest NAEP scaled score unit.
For Smarter Balanced, PARCC, and ACT Aspire, the aggregate state-level proportion at and above the cut $c$ is $\hat{p}_{c}$ with standard error $\hat{\sigma}_{\hat{p}_{c}}$ and was based on the weighted average of the states and jurisdictions within the consortium. The weights were the population sizes within each state. For Smarter Balanced, PARCC, and ACT Aspire, the state NAEP aggregate scores $\hat{S}_{N}$ were estimated with the NCES NDE (http://nces.ed.gov/nationsreportcard/naepdata/).

B Aggregate Smarter Balanced results are based on the weighted average of 18 states: California, Connecticut, Delaware, Hawaii, Idaho, Maine, Michigan, Missouri, Montana, Nevada, New Hampshire, North Dakota, Oregon, South Dakota, Vermont, Washington, West Virginia, and Wisconsin. For ELA, Missouri and Wisconsin were excluded because they did not follow the Smarter Balanced blueprint.
ß Aggregate PARCC results are based on the weighted average of 12 jurisdictions: Arkansas, Colorado, District of Columbia, Illinois, Louisiana, Maryland, Massachusetts, Mississippi, New Jersey, New Mexico, Ohio, and Rhode Island. In grade 8 mathematics, in some PARCC states, some students took the Algebra 1 test. In the mapping study, this factor could have had the effect of making the grade 8 mathematics PARCC standards appear higher.
B Aggregate ACT Aspire results are based on the weighted average of two jurisdictions: Alabama and South Carolina.

# 昰AIR <br> AMERICAN INSTITUTES FOR RESEARCH* 

1000 Thomas Jefferson Street NW
Washington, DC 20007-3835
202.403.5000 | TTY: 877.334.3499
www.alr.org

## Making Research Relevant


[^0]:    ${ }^{1}$ A recent study for mathematics by the NAEP Validity Study (NVS) panel found that $79 \%$ of NAEP items were matched to content in the CCSS in the $4^{\text {th }}$ grade and $87 \%$ in the $8^{\text {th }}$ grade (Daro, Hughes and Stancavage, 2015).

